

**National Examinations - May 2018**  
**16-Mec-A5, Electrical & Electronics Engineering**  
**Mechanical Engineering**

3 hours duration

---

Name [print]:

Signature:

---

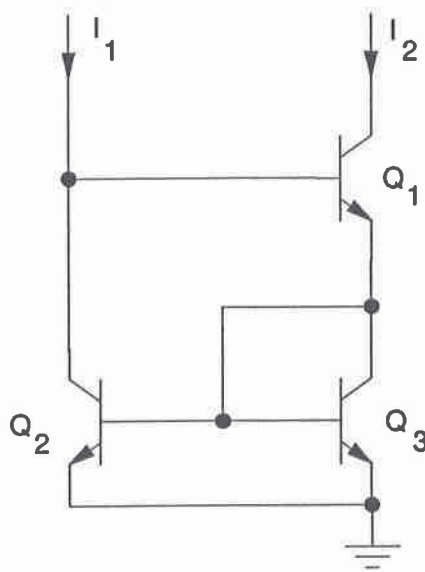
Notes:

- [1] If doubt exists as to the interpretation of any question, the candidate is urged to submit, with the answer paper, a clear statement of any assumptions made.
- [2] Candidates may use one of two calculators, the Casio or Sharp approved models. This is a closed book examination.
- [3] This examination consists of the front page and 8 numbered pages.
- [4] Any five (5) questions constitute a complete paper. Only the first five questions as they appear in your answer book will be marked.
- [5] Each question is of equal value.
- [6] Clarity and organization of answers are important.
- [7] The candidate is required to sign this examination paper and submit it with the solution booklets.
- [8]  $\pi = 3.14159$   
 $1 \text{ hp} = 746 \text{ W}$   
 $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$

**QUESTION 1**

Consider the transistor circuit shown in Figure 1. All transistors can be assumed to be identical with a dc current gain  $\beta$ .

Calculate the current transfer ratio for the circuit,  $I_2 / I_1$ , as a function of  $\beta$ .



**Figure 1** Transistor Circuit

## QUESTION 2

This question consists of two parts which are not necessarily related.

### Part I

A combinational logic circuit is shown in Figure 2.

- Write a general Boolean algebra expression for the output F as a function of the inputs A, B.
- Using DeMorgan's theorems and other Boolean identities, simplify the expression obtained in [a]. Is there a single gate which can replace the network shown?
- Generate a truth table giving the logic levels at points C, D, E and F for inputs A, B.

### Part II

Design a 2-input exclusive or (EOR) gate using only 2-input NOR gates.

- Develop the truth table for the gate.
- Write a general Boolean algebra expression for the output as a function of the inputs.
- Using DeMorgan's theorems and other Boolean identities, modify the expression obtained in [e] to provide a solution which can be implemented with NOR gates.
- Draw the circuit diagram for the final gate array.

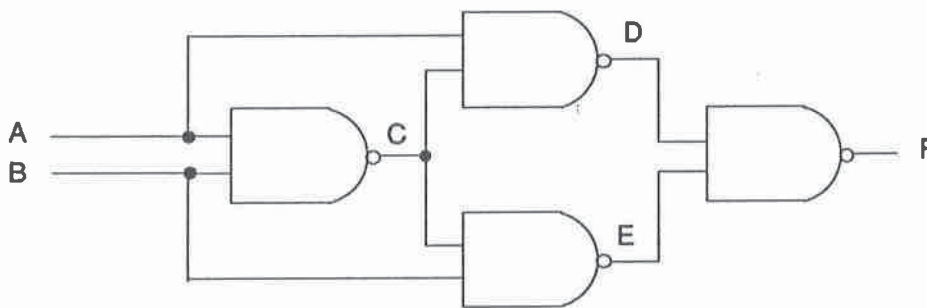


Figure 2 Combinational Logic Circuit

## QUESTION 3

A linear dc machine consisting of a conducting bar resting on two conducting rails is shown in Figure 3. The magnetic flux density is 1 T, directed into the page, the resistor  $R$  is  $0.05\Omega$ , the rail separation is 1 metre, and the battery voltage  $V_0$  is 2 V. Assume negligible friction between the bar and rails.

- [a] Assume that the bar is stationary at time  $t=0$  when the switch  $S_1$  is closed. What is the magnitude and direction of the force on the bar at the start? What is the initial current flow? What is speed of the bar assuming that no mechanical load is applied to the bar?
- [b] If the bar is loaded down with a force of 20 N opposite to the direction of motion, determine the new steady state speed. Calculate the power delivered by the battery, the power delivered to the mechanical load and the power lost to heat in the resistance  $R$ . What is the efficiency of the machine under these circumstances?
- [c] The loading force in part [b] is removed and a mechanical pulling force of 10 N directed to the right is applied to the bar. In steady state, determine the speed, the power taken from the mechanical source, the power delivered to the battery and the power lost to heat in the resistance  $R$ . What is the efficiency of the machine under these circumstances?

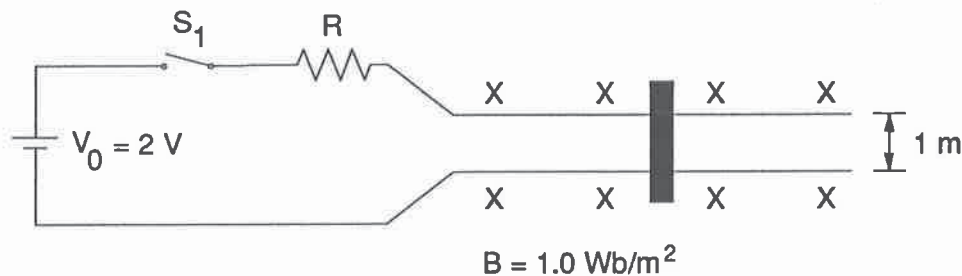


Figure 3 Top View of Linear dc Machine

## QUESTION 4

Consider the magnetic circuit of a transformer shown in Figure 4. Infinite relative permeability can be assumed for the iron core.

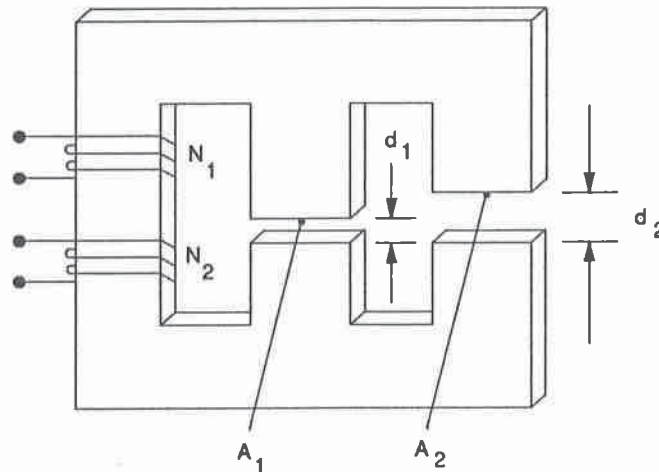


Figure 4 Transformer

The following specifications apply.

$L_1$	$3.77 \times 10^{-2} \text{ m}$	$A_1$	$0.02 \text{ m}^2$
$L_2$	$7.54 \times 10^{-2} \text{ m}$	$A_2$	$0.02 \text{ m}^2$
$N_1$ [primary]	200 turns	$N_2$ [secondary]	20 turns

When a dc voltage equal to 10 mV is applied to the primary, the measured primary current is 100 mA. When a dc voltage of 0.1 mV is applied to the secondary winding, the measured secondary current is 100 mA.

Assume that leakage inductances and eddy current and hysteresis losses are negligible; consider an operating frequency of 1000 Hz.

- Draw the equivalent circuit of the transformer referred to the primary and calculate component values.
- A transducer with an impedance of  $0.078 \Omega$  is connected across the secondary of the transformer; an amplifier is connected to the primary. Calculate the output impedance of the amplifier to give maximum power transfer to the load.

## QUESTION 5

Consider the circuit shown in Figure 5 which has been designed using ideal operational amplifiers ( $U_1$  to  $U_3$ ) with infinite bandwidth and infinite open loop gain. In the schematic,  $a$ ,  $b$  and  $c$  are constants. You will note that  $U_3$  is configured as a basic difference amplifier which has a transfer function given by:

$$E_0 = c (e_y - e_x)$$

where  $e_y$  and  $e_x$  are the potentials at points  $y$  and  $x$  respectively.

In the derivation of the transfer function for such circuits, one can assume:

- [i] Zero differential voltage between the input terminals of the operational amplifier,
- [ii] Zero current flows into either input terminal of the operational amplifier.

Applying the principle of superposition, derive an expression for the transfer function of the total circuit [ $E_0$  as a function of  $E_1$ ,  $E_2$ ].

**Hint:** Let  $E_2 = 0$ , and solve for the potentials at points  $x$  and  $y$  for input  $E_1$ .  
Let  $E_1 = 0$ , and again solve for the potentials at points  $x$  and  $y$  for input  $E_2$ .  
Calculate the resultant output  $E_0$  for both  $E_1$  and  $E_2$  inputs.

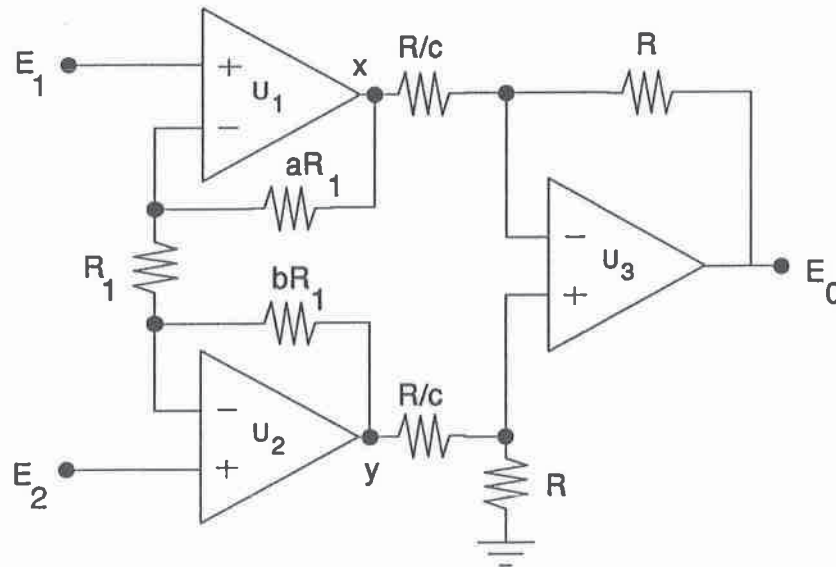


Figure 5 Circuit Schematic

## QUESTION 6

### Part I

A dc test is performed on a 208-V, six-pole, delta connected, 60Hz induction motor, as shown in Figure 6.

[a] If  $V_{DC} = 3.32 \text{ V}$  and  $I_{DC} = 3.1 \text{ A}$ , calculate the per phase stator resistance,  $r_1$ .

Three phase excitation is applied to the motor which runs with a slip of 3.5%. Find:

[b] The speed of the magnetic field in revolutions per minute.

[c] The speed of the rotor in revolutions per minute.

[d] The electrical frequency of the rotor current.

The load on the motor is now doubled. Calculate:

[e] The speed of the rotor in revolutions per minute.

### Part II

You are provided with a graph of the speed-torque characteristic of a three phase wound rotor induction motor. The torque required to drive a pump is  $T = K_p n^2$  ( $K_p$  is a constant;  $n$  is speed in revolutions/second). The induction motor is to be used to drive the pump. Show how you would determine the operating point speed of the system.

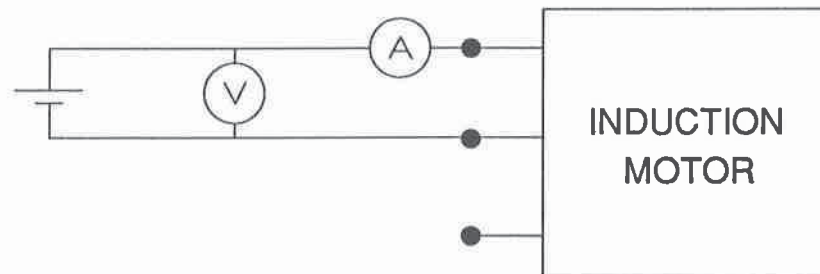


Figure 6 dc Test on Induction Motor

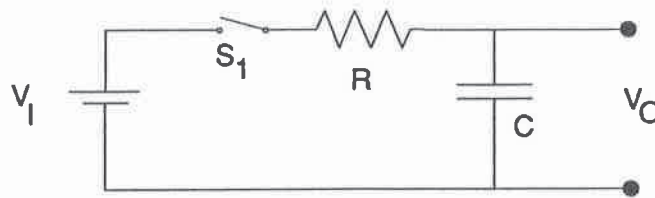
## QUESTION 7

Consider the RC circuit shown in Figure 7[a]. The switch  $S_1$  is closed at time  $t=0$  connecting the dc supply  $V_I$  to the network.

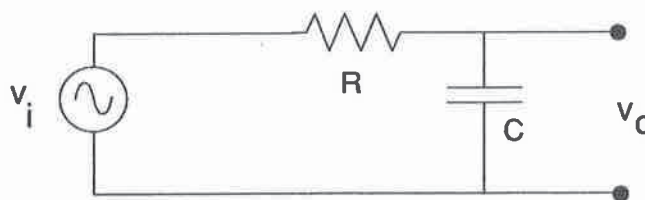
- [a] Derive an expression for the transfer function of the circuit,  $V_o/V_I$ , in the time domain.
- [b] Sketch the transfer function for a time interval of 5 time constants.

The RC circuit is reconfigured as shown in Figure 7[b]. An ac voltage source of variable frequency  $v_i$  is connected to the input.

- [c] Derive an expression for the transfer function of the circuit,  $v_o/v_i$ , in the frequency domain.
- [d] Sketch the magnitude of the transfer function for a frequency range of 4 decades centered at the corner frequency of the circuit.



[a]



[b]

Figure 7 RC Circuit: [a] dc test; [b] ac test



## QUESTION 8

An industrial load is represented in Figure 8 by  $R = 6\Omega$  and  $X_L = 8\Omega$ . The load voltage is  $250\angle 0^\circ$  V.

- Calculate the load current, power, reactive power and power factor.
- Calculate the generator voltage  $V_G$  required at the input end of the transmission line (represented by the series impedance  $Z_T = (1 + j3)\Omega$ ) and the power lost in transmission  $P_T$ .
- If capacitor  $X_C = 12.5\Omega$  is connected in parallel by closing switch S, calculate  $I_C$ , the new load current I, and the new power factor. Show V,  $I_L$ ,  $I_C$ , and I on a phasor diagram.
- Calculate the new generator voltage and the new transmission power loss.
- What two advantages do you see for improving the power factor by adding a parallel capacitor?

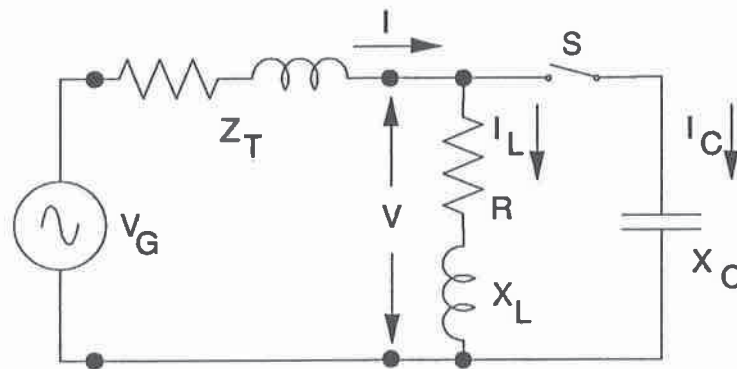


Figure 8 Industrial Load