## 07-Mec-A6-2 Advanced Strength of Materials

3 Hours Duration

## NOTES:

1. If doubts exist as to the interpretation of any question, the candidate is urged to submit with the answer paper, a clear statement of any assumptions made.
2. Any non-communicating calculator is permitted. This is an open book exam.
3. Any five of the eight problems constitute a complete paper. If you choose to attempt more than five problems, only the first five problems as they appear in your answer book will be marked.
4. All problems are of equal value.

1- Using an energy method, determine the displacement of point $B$ of the beam shown below. Take $\mathrm{E}=200 \mathrm{GPa}, \mathrm{I}=185 \times 10^{6} \mathrm{~mm}^{4}$.


2- The two uniform linearly elastic rods shown below are welded together at $B$, and the resulting two-segment rod is attached to rigid supports at A and C . Rod (I) has a modulus $\mathrm{E}_{1}=180 \mathrm{GPa}$, cross-sectional area $\mathrm{A}_{1}=550 \mathrm{~mm}^{2}$, length $\mathrm{L}_{1}=150 \mathrm{~mm}$, and coefficient of thermal expansion $\alpha_{1}=8 \times 10^{-5} /{ }^{\circ} \mathrm{C}$. Rod (2) has a modulus $\mathrm{E}_{2}=90 \mathrm{GPa}$, cross-sectional area $A_{2}=900 \mathrm{~mm}^{2}$, length $L_{2}=100 \mathrm{~mm}$, and coefficient of thermal expansion $\alpha_{2}=17 \times 10^{-6} /{ }^{\circ} \mathrm{C}$.
a) Determine the axial stresses in the rods if the temperature of both is raised by $50^{\circ} \mathrm{C}$.
b) Determine whether joint $B$ moves to the right or left and by how much?


3- A bar of solid circular cross-section of 50 mm diameter is subjected to a torque, $T$, and an axial tensile load, P. A rectangular strain gauge rosette attached to the surface of the bar gives the following strain readings: $\varepsilon_{0}=80010^{-6}, \varepsilon_{45}=-200 \times 10^{-6}$ and $\varepsilon_{90}=-400 \times 10^{-6}$ with the 0 degree gauge being aligned with the axial direction of the bar. If Young's modulus, E , for the bar is 80 GPa and Poisson's ratio, $v$, is 0.28 , calculate the values of T and P .

4- A thick-walled cylinder with 0.10 m internal diameter and 0.15 m external diameter is fabricated of a material whose elastic limit is 340 MPa and Poisson's ratio $v=0.32$. The cylinder is subjected to an internal pressure 3.5 times greater than the external pressure. Calculate the allowable internal pressure according to:
a) the maximum shear stress criterion, and
b) the Von-Mises criterion.

5- A two-dimensional strain field is given by

$$
\varepsilon_{x}=c\left(-18 x^{2}+42 y^{2}\right) \quad \varepsilon_{y}=c\left(6 x^{2}-30 y^{2}\right) \quad \gamma_{x y}=6 b x y
$$

where $b$ and c are nonzero constants.
a) What is the relationship between $b$ and $c$ for this field to satisfy the strain compatibility conditions?
b) Determine the displacements $\mathrm{u}(\mathrm{x}, \mathrm{y})$ and $\mathrm{v}(\mathrm{x}, \mathrm{y})$ corresponding to this field of strain.

6- A thin square plate of one meter by one meter is subjected to a state of plane stress represented by uniform normal stresses $\sigma_{x}$ and $\sigma_{y}$ as illustrated below. All other stresses are zero. The two stresses shown cause the plate to elongate by 0.4 mm in the x direction and by 0.1 mm in the y direction. If it is known that $\sigma_{\mathrm{y}}$ is equal to 100 MPa and E is equal to 80 GPa and that all deformations are in the linear-elastic range, determine:

a) $\sigma_{x}$
b) the Poisson's ratio for the material from which the square is made, and
c) the strain in the thickness direction (z-direction).

7- A pin-ended column of height 2.0 m has a circular cross-section of diameter 60 mm , wall thickness 2.0 mm and is converted to an open section by a narrow longitudinal slit; the ends of the column are free to warp. If the column is made from materials with $E=50$ GPa and $G=15 \mathrm{GPa}$, determine the values of axial load which would cause the column to buckle in:
a) pure bending mode
b) pure torsion mode

8- Calculate the forces in the members $\mathrm{FG}, \mathrm{GD}$ and CD of the truss shown in the figure below using the principle of virtual work. All horizontal and vertical members are 1 m long.


