NOTES:

1.   If doubt exists as to the interpretation of any question, the candidate is urged to submit with the answer paper a clear statement of any assumption made.

2.   Each candidates may use an approved model of a Casio or Sharp calculator; otherwise, this is a CLOSED BOOK Examination.

3.   Answer BOTH questions #1, and #2. Answer ONLY TWO of questions #3, #4, or #5. Answer ONLY TWO of questions #6, #7, #8 OR #9. SIX questions constitute a complete paper.

4.   The marks assigned to each question are shown in the left margin.

FRONT PAGE

QUESTION #1 MUST BE ANSWERED.

(8)   1.   Indicate with arrows (⟲ a rotation; ⟶ a translation) on each structure and list beside each structure the number of structural degrees of freedom that are required to do an analysis by the slope-defection method. In each case, use the minimum number of structural degrees of freedom; where they occur, take into account symmetry, anti-symmetry and joints that are known to have zero moments.
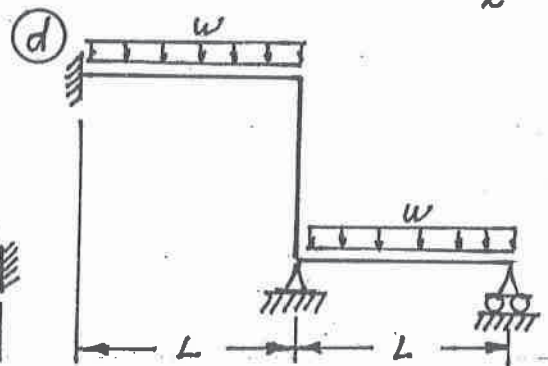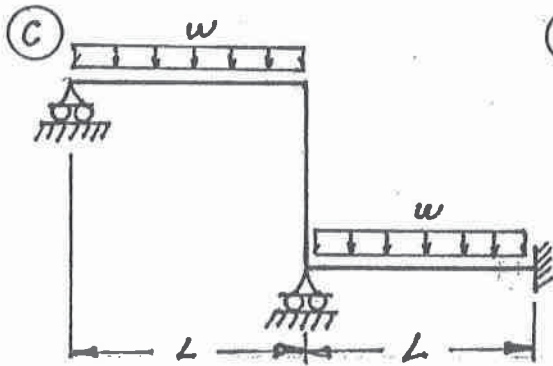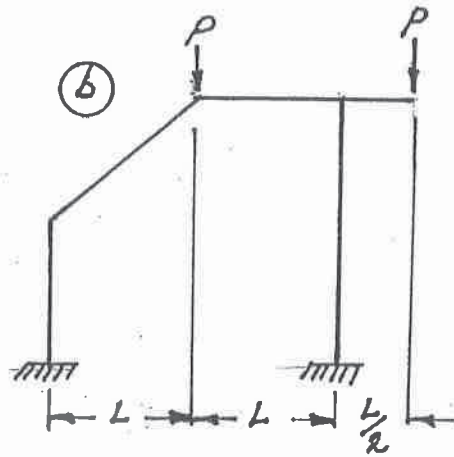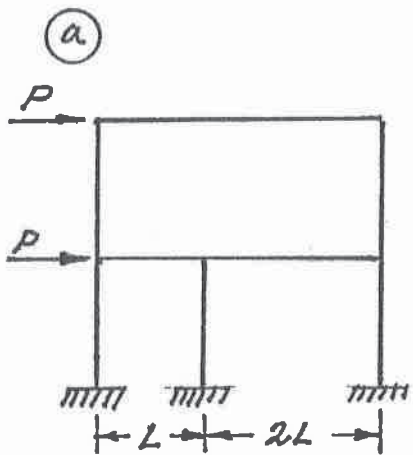
(12)   2.   Schematically show the shear force and bending moment diagrams for the following
                structures. All members have the same EI and are inextensible.
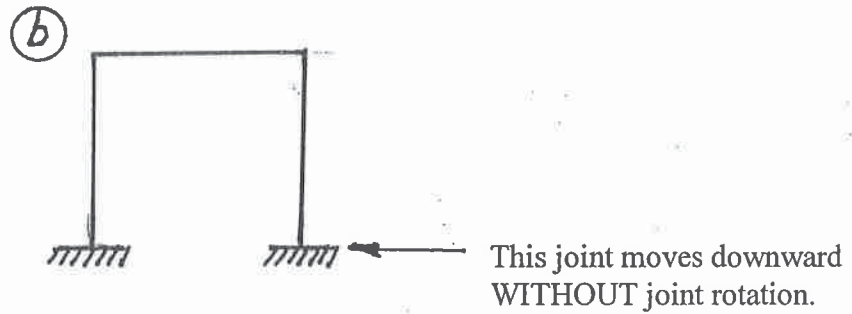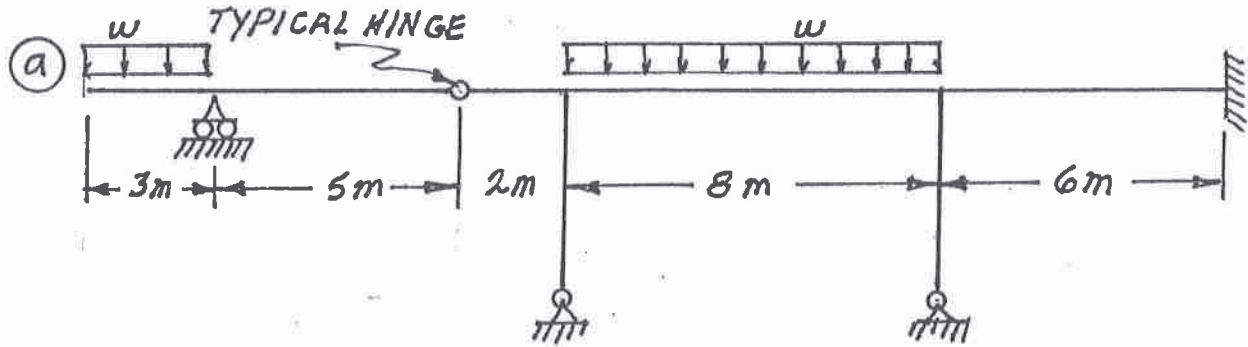
SELECT AND ANSWER TWO QUESTION ONLY FROM QUESTIONS 3, 4, OR 5.

(16)   3.   Use Castigliano's theorem (the least work theorem) to analyze the structure shown.
                Calculate the bending moment and shear on the beam at joint ①. Both members have the
   same EI value and are inextensible.
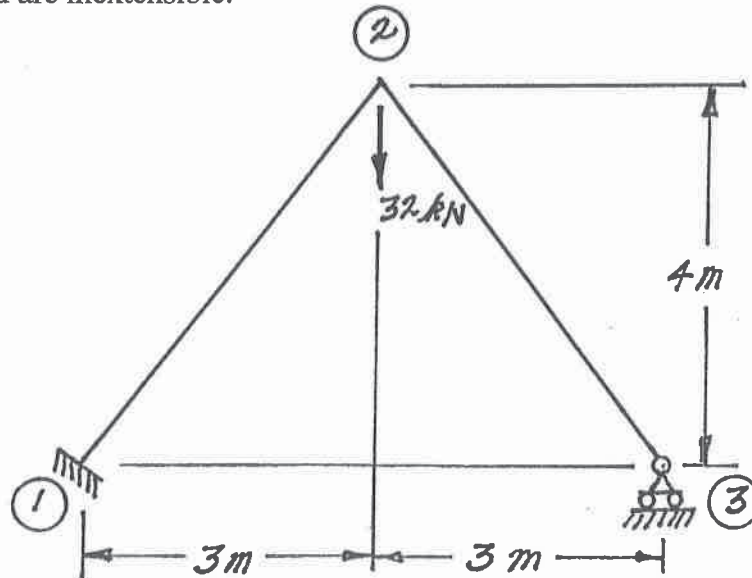
SELECT AND ANSWER TWO QUESTION ONLY FROM QUESTIONS 3, 4, OR 5.

(16)   4.   Loads are applied to the bottom chord of the pin-jointed truss shown below. Draw
influence lines for forces in the following members and calculate and indicate the
maximum ordinate value on each influence line:

a) U_4U_5
b) U_2L_3
c) U_1U_2
d) U_4L_5
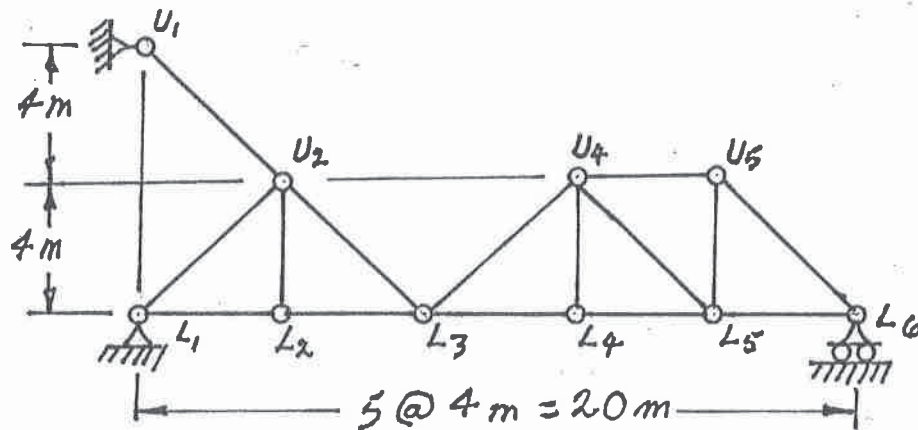
(16)   5.   Use the slope-defection or the moment-distribution method to analyze the frame
structure shown. Draw shear and bending moment diagrams. For each member on
both diagrams, indicate the magnitude of maximum and minimum ordinates
(Minimum ordinates are frequently negative values). There are no loads on the
structure, but because of temperature change the centre line of each member
increases in length by 0.006 m. Neglect the strains caused by axial stresses and
take advantage of symmetry. All members of the structure have the same EI value
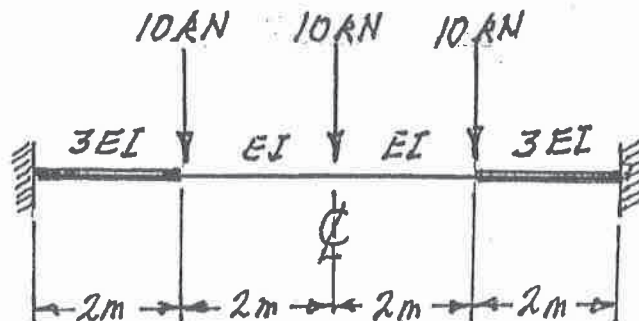which is 2.1×10^5 kN.m^2.
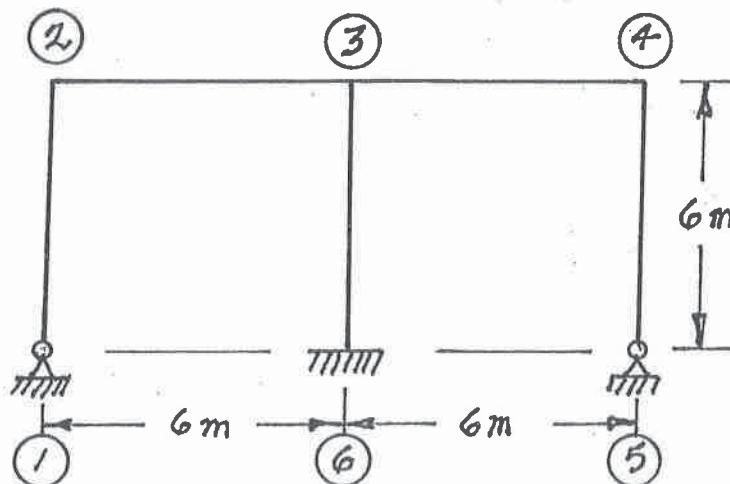
SELECT AND ANSWER TWO QUESTIONS ONLY FROM QUESTIONS 6, 7, 8 OR 9.

(24) 6.   Using the slope-defection method or the moment-distribution method, analyze the frame shown. In addition to the effects of the uniformly distributed loading, stresses and strains are caused because the right support moved outward 16 mm as shown. Draw shear force and bending moment diagrams. On each diagram for each member, indicate the magnitudes of the maximum and minimum ordinates (Minimum ordinates are frequently negative values). Both members are inextensible and have the relative EI values shown; $EI = 10,000 \text{ kN.m}^2$.
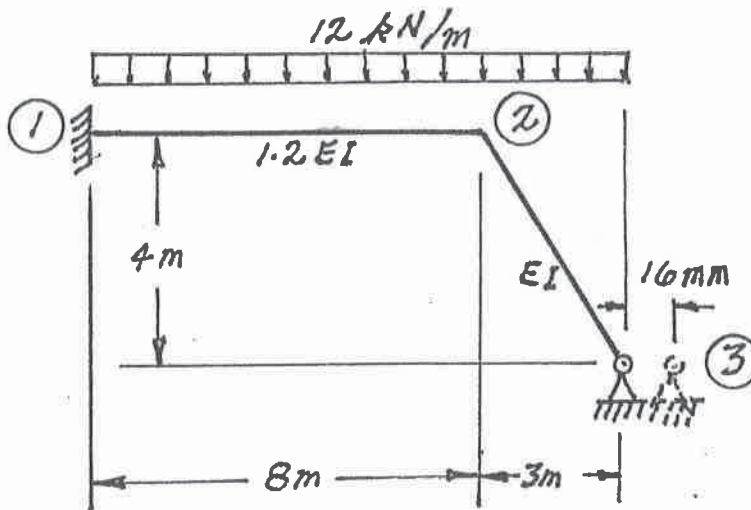

(24) 7.   Using a **flexibility (force) method**, determine the fixed-end moments for the non-prismatic beam with the three point loads shown. Take advantage of symmetry.

SELECT AND ANSWER TWO QUESTION ONLY FORM QUESTIONS 6, 7, 8 OR 9.

(24)   8.   Using the slope-defection method, analyze the frame structure shown below. Plot shear force and bending moment diagrams. For each member on each diagram, indicate the magnitude of the maximum and minimum ordinates (Minimum ordinates are frequently negative values). All members are inextensible and have the same EI value. Take advantage of anti-symmetry where it applies.
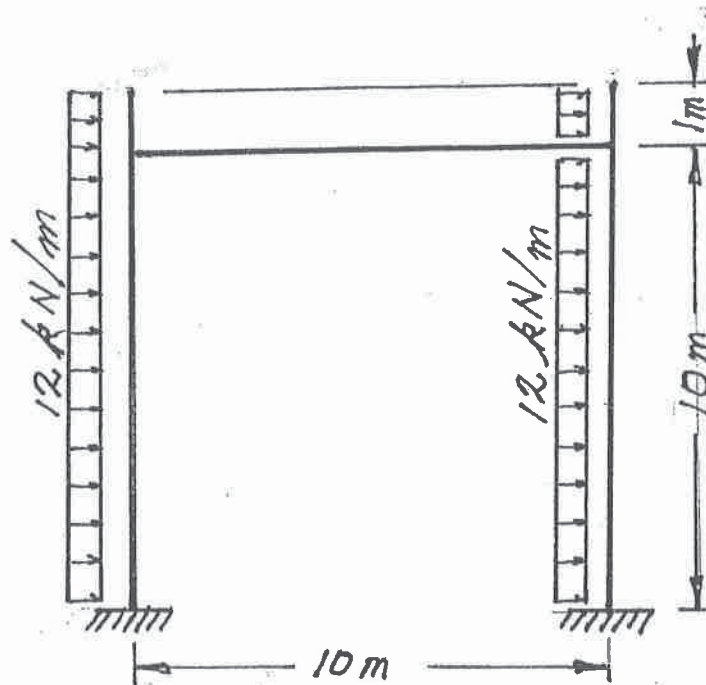
(24)   9.   a)   For the frame shown, derive the equilibrium equation for translation at
                    joint ② Neglect the effects of axial strain. All members have the same EI value.

        b)   Derive the equilibrium equations for moment equilibrium at joints ② and ③.

        c)   Present your results in matrix form by giving the terms of the stiffness matrix [K]
              and the load vector {P} in the following equation:

$$[K] \begin{Bmatrix} \delta \\ \theta_2 \\ \theta_3 \end{Bmatrix} = \{P\}$$

DO NOT SOLVE THE EQUATIONS.

The unknowns of the problem shall be:

δ = translation at joint ② (positive in the direction shown)

θ_2 = rotation of joint ②

θ_3 = rotation of joint ③

(counter clockwise positive)