

NATIONAL EXAMS MAY 2016

07-Str-A4 ADVANCED STRUCTURAL ANALYSIS

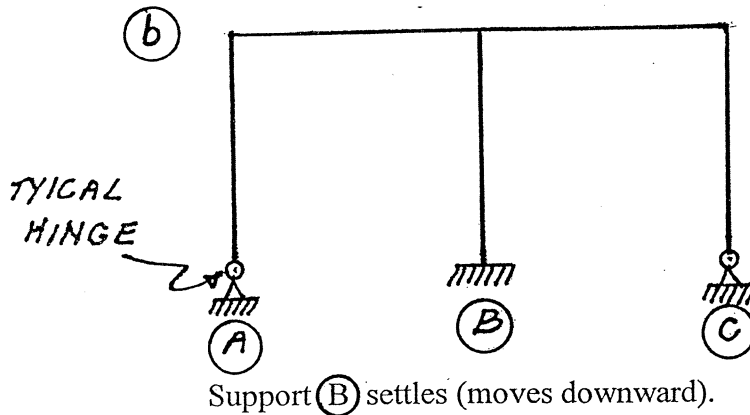
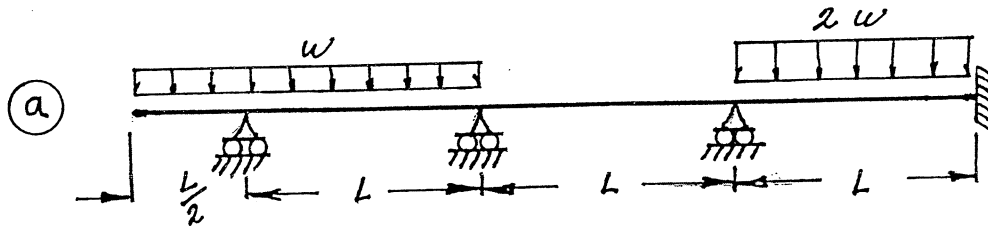
3 HOURS DURATION

NOTES:

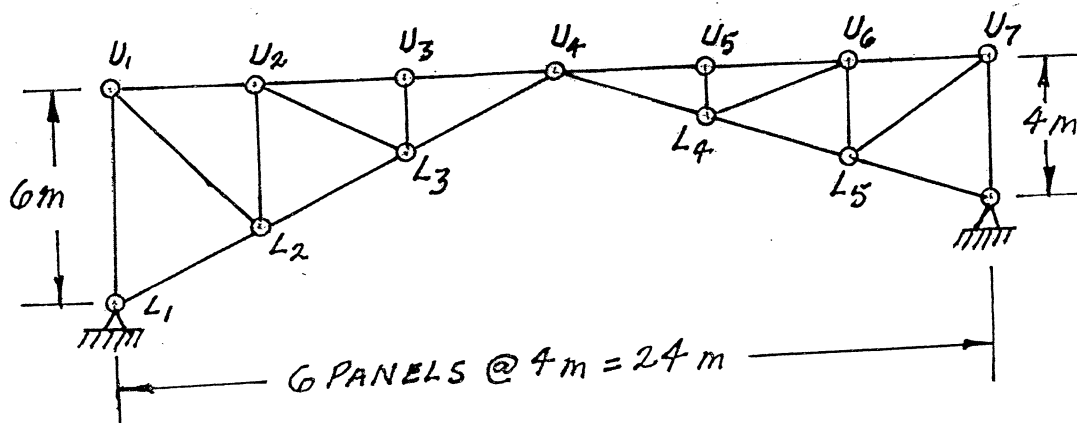
1. If doubt exists as to the interpretation of any question, the candidate is urged to submit with the answer paper a clear statement of any assumption made.
2. Each candidate may use an approved model of Sharp or Casio calculator; otherwise, this is a CLOSED BOOK Examination.
3. Answer BOTH questions #1, and #2. Answer ONLY TWO of questions #3, #4, or #5. Answer ONLY TWO of questions #6, #7 or #8. SIX questions constitute a complete paper.
4. The marks assigned to each question are shown in the left margin.

QUESTIONS #1 AND #2 MUST BE ANSWERED.

- (8) 1. Schematically show the shear force and bending moment diagrams for the following structures. All members have the same EI and are inextensible.

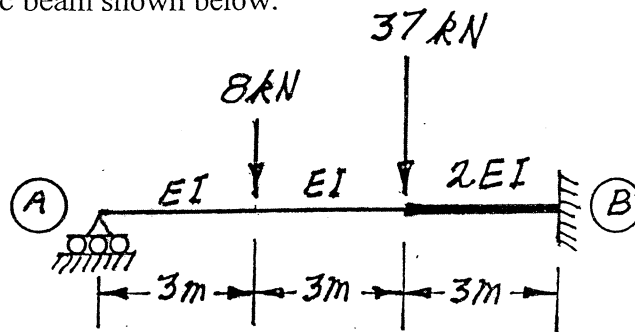


- (8) 2. For a load applied to the top chord of the pin-jointed truss shown below, schematically show the influence line for the force in the following members:
- a)  $U_2 - L_3$
  - b)  $L_1 - L_2$

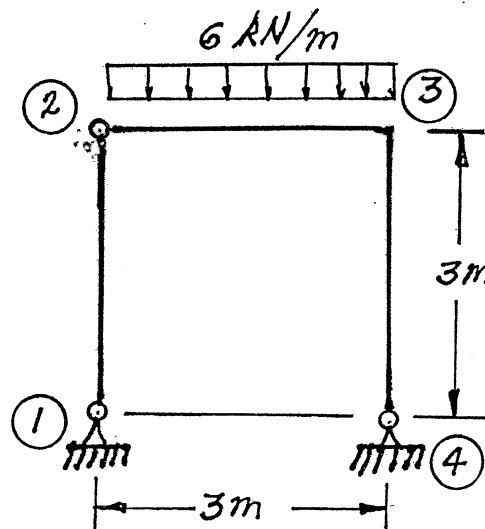


SELECT AND ANSWER TWO QUESTION ONLY FROM QUESTIONS #3, #4, OR #5.

- (21) 3. Using a **flexibility (force) method**, determine the fixed-end moment at the right end of the non-prismatic beam shown below.

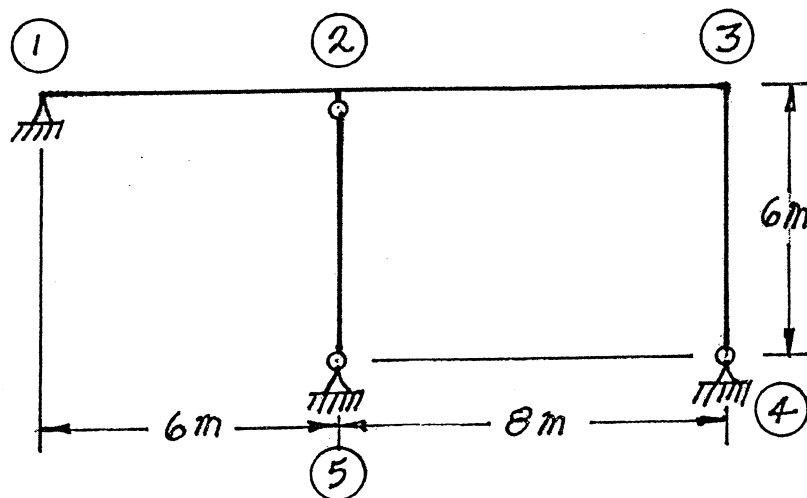


- (21) 4. Use Castigliano's theorem to determine the horizontal deflection at joint ② of the frame shown below. All members are inextensible and have the same EI value.  $EI = 2.5 \times 10^4 \text{ kN.m}^2$ .



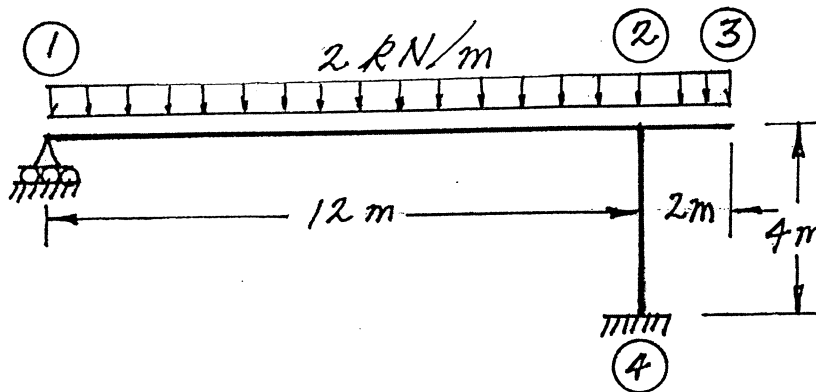
SELECT AND ANSWER TWO QUESTION ONLY FROM QUESTIONS #3, #4, OR #5.

- (21) 5. Use the slope-deflection method or the moment-distribution method to analyze the frame structure shown. Draw shear and bending moment diagrams. For each member, indicate on both diagrams the magnitudes of maximum and minimum ordinates (Minimum ordinates are frequently negative values). There are no loads on the structure, but member ②–⑤ was fabricated exactly 0.06 m too long; the member was forced into place after all other members were erected. All members of the structure are inextensible and have the same EI value which is  $6.0 \times 10^4 \text{ kN.m}^2$ .



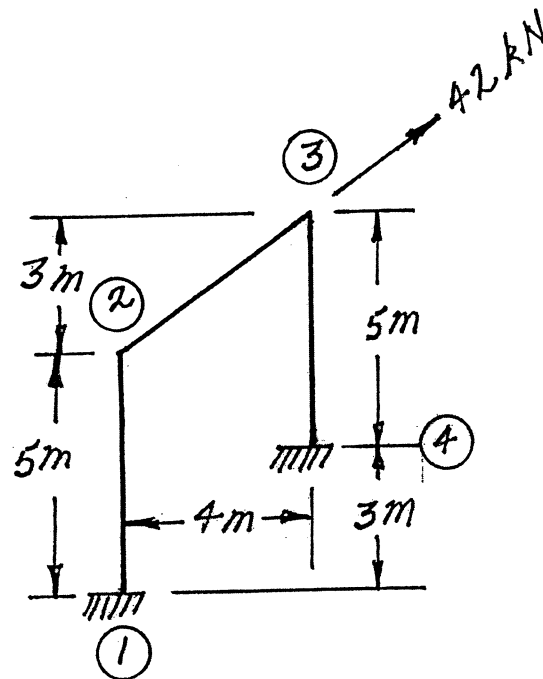
SELECT AND ANSWER TWO QUESTIONS ONLY FROM QUESTIONS #6,#7 OR #8.

- (21) 6. Using the slope-deflection method, analyse the structure shown. Draw shear force and bending moment diagrams. On each diagram for each member, indicate the magnitudes of the maximum and minimum values (Minimum values are often negative). All members are inextensible and have the same EI value. Horizontal motion is not prevented at joints (1), (2) or (3).



SELECT AND ANSWER TWO QUESTIONS ONLY FROM QUESTIONS #6,#7 OR #8.

- (21) 7. Using the slope-deflection method or the moment-distribution method, analyse the structure shown below. Plot shear force and bending moment diagrams. On each diagram for each member, indicate the magnitudes of the maximum and minimum values (Minimum values are often negative). All members are inextensible and have the same EI value.



- (21) 8. a) For the frame shown, derive the equilibrium equation for the translation shown at joint ③. Neglect the effects of axial strain. EI has the same value for both members.
- b) Derive the equilibrium equations for moment equilibrium at joints ② and ③.
- c) Present your results in matrix form by giving the terms of the stiffness matrix [K] and the load vector {P} in the following equation:

$$[K] \begin{Bmatrix} \delta \\ \theta_2 \\ \theta_3 \end{Bmatrix} = \{P\}$$

**DO NOT SOLVE THE EQUATIONS.**

The unknowns of the problem shall be:

$\delta$  = translation at joint ③ (positive to the right)

$\theta_2$  = rotation of joint ②

(counter clockwise positive)

$\theta_3$  = rotation of joint ③

