

National Exam, December, 2018

16-Elec-A1 Circuits

3 hours duration

NOTES:

1. **No questions to be asked.** If doubt exists as to the interpretation of any question, the candidate is urged to submit with the answer paper, a clear statement of any logical assumptions made.
2. Candidates may use one of two calculators, a Casio or Sharp approved model . **No programmable models** are allowed.
3. This is a **closed book** examination.
4. Any **five questions** constitute a complete paper. Please **indicate in the front page of your answer book which questions you want to be marked.** *If not indicated, only the first five questions as they appear in your answer book will be marked.*
5. All questions are of equal value. **Part marks will be given for right procedures.**
6. **Some useful equations and transforms** are given in the last page of this question paper.

- Q1: For the circuit shown in Figure-1,
- (a) Calculate the equivalent resistance of the circuit, R_{AB} at the terminals A and B. [10]
 - (b) Solve for the current I at the location shown. [5]
 - (c) Calculate the Power dissipation in the 12Ω resistance. [5]

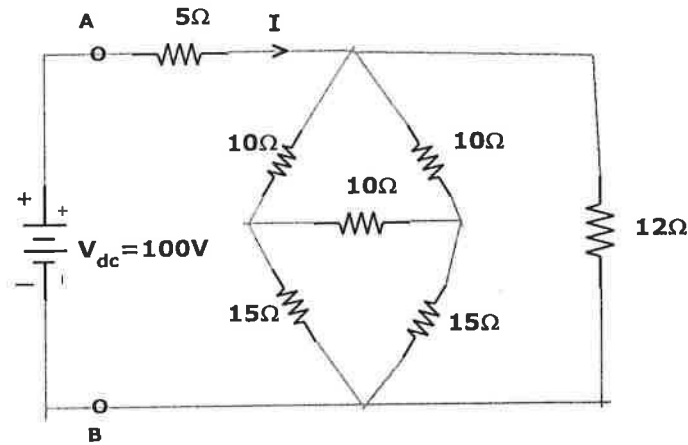


Figure-1

- Q2: In the Figure-2 solve the voltage, V_o by the Superposition theorem. [20]

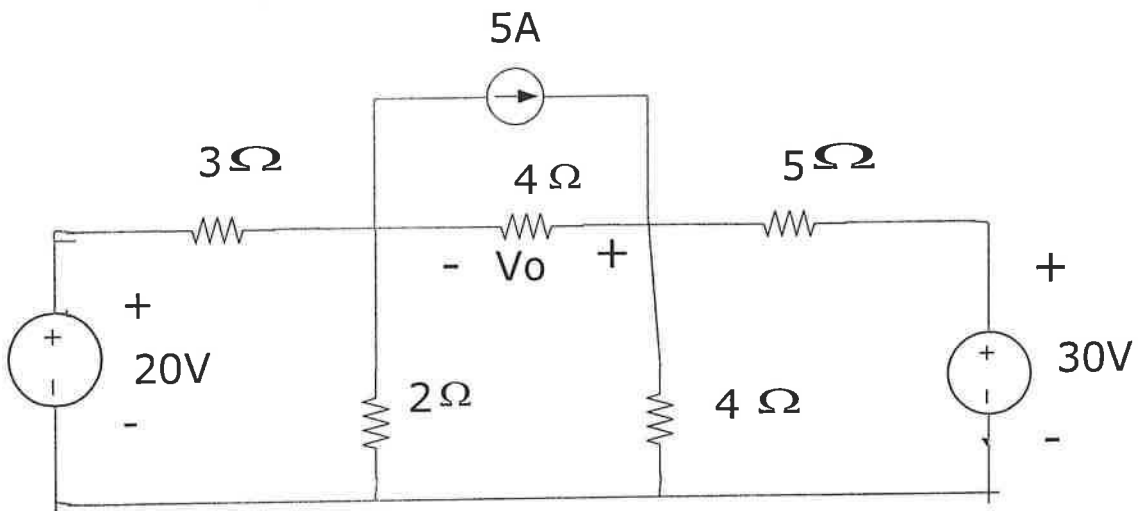


Figure-2

Q3: In Figure-3, the switch was in position-A for a long time. At $t = 0$, it is moved to Position-B.

Calculate (i) $v_c(0+)$, $\frac{dv_c}{dt}(0+)$, and $v_c(\infty)$ [4+6+2]

(ii) $v_c(t)$ when $t \geq 0$ [8]

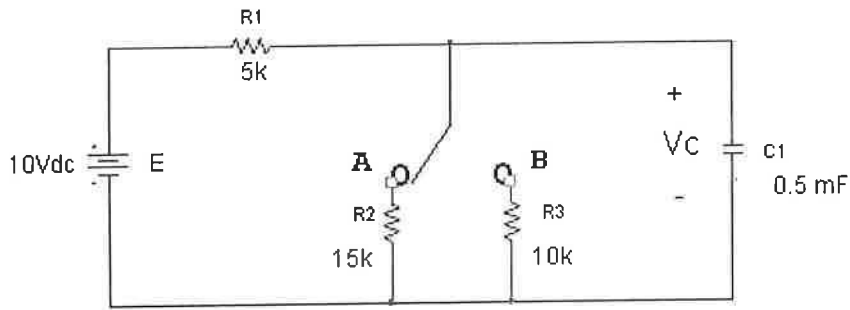


Figure-3

Q4: (a) For the circuit shown in Figure-4, calculate the load resistance R_L to be connected across the terminals a and b for maximum power dissipation. [10]

(b) Calculate this maximum possible power dissipation in R_L . [10]

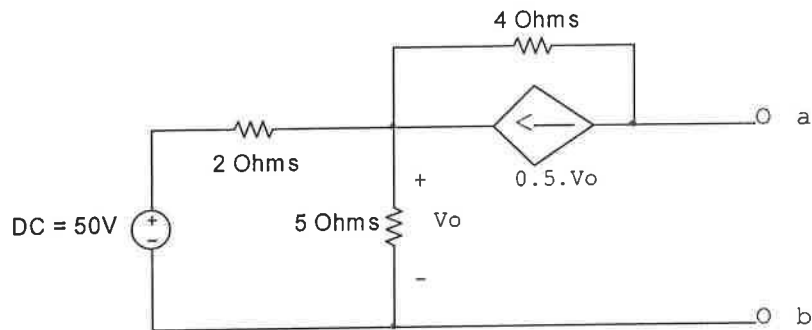


Figure-4

- Q5: (a) Write the Node Voltage equations of the following ac circuit, Figure-5, where the frequency is 60 Hz. [8]
- (b) Solve the node voltages, and calculate the power supplied by the voltage source, e. [6+6]

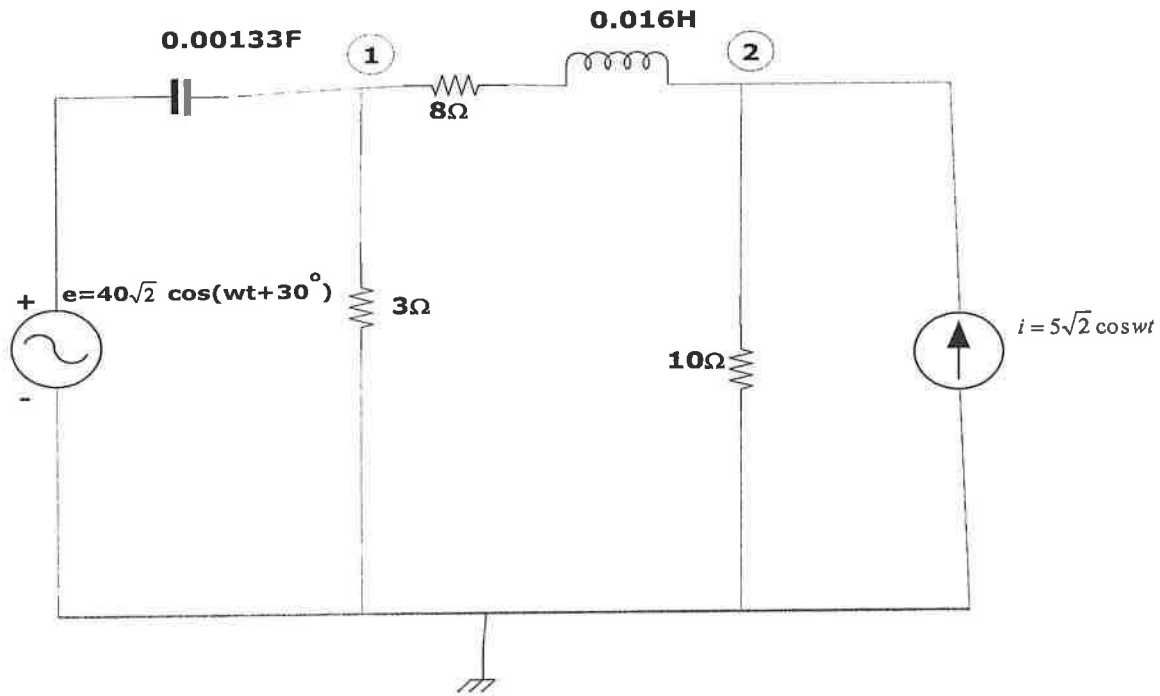


Figure-5

- Q6: (a) In the circuit shown in Figure-6, the switch was on position-a for a long time. At $t = 0$, the switch is moved to position-b. Calculate $V_c(0^+)$ and $i(0^+)$. [4]
- (b) Draw the Laplace Transformed circuit at $t \geq 0$. [8]
- (c) Solve $V_c(t)$. [8]

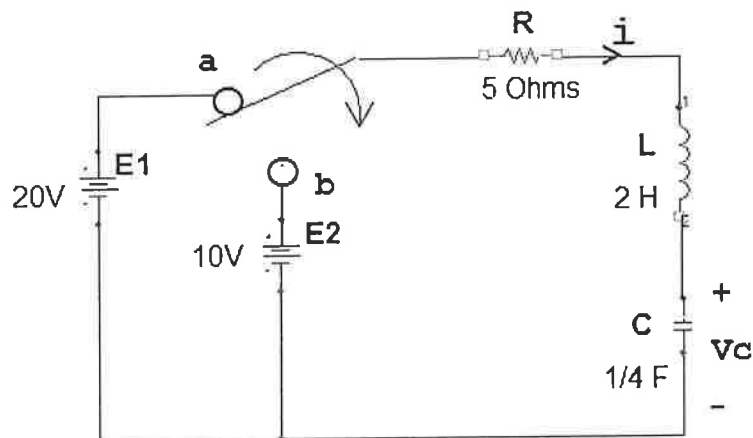


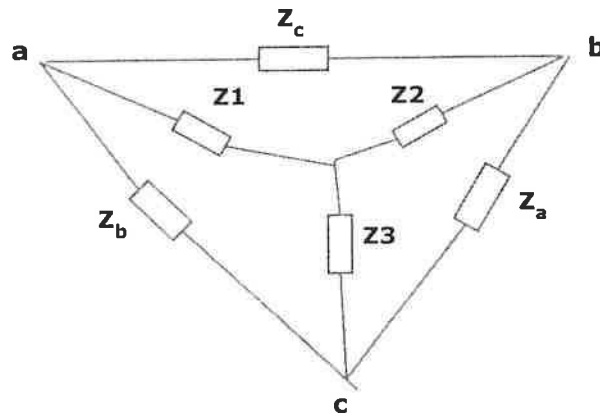
Figure-6

Appendix

Some useful Laplace Transforms:

<u>f(t)</u>	→	<u>F(s)</u>
Ku(t)		K / s
$\delta(t)$		1
t		1/s ²
e ^{-at} u(t)		1 / (s+a)
sin wt . u(t)		w / (s ² +w ²)
cos wt . u(t)		s / (s ² +w ²)
e ^{-at} sin wt		$\frac{\omega}{(s+\alpha)^2+\omega^2}$
e ^{-at} cos wt		$\frac{(s+\alpha)}{(s+\alpha)^2+\omega^2}$
$\frac{df(t)}{dt}$		s F(s) – f(0 ⁻)
$\frac{d^2 f(t)}{dt^2}$		s ² F(s) – s f(0 ⁻) – f'(0 ⁻)
$\int_{-\infty}^t f(q) dq$		$\frac{F(s)}{s} + \int_{-\infty}^0 f(q) dq$

Star – Delta conversion:



$$Z_1 = \frac{Z_b \cdot Z_c}{Z_a + Z_b + Z_c}$$

$$Z_2 = \frac{Z_a \cdot Z_c}{Z_a + Z_b + Z_c}$$

$$Z_3 = \frac{Z_a \cdot Z_b}{Z_a + Z_b + Z_c}$$

$$Z_a = \frac{Z_1 \cdot Z_2 + Z_2 \cdot Z_3 + Z_3 \cdot Z_1}{Z_1}$$

$$Z_b = \frac{Z_1 \cdot Z_2 + Z_2 \cdot Z_3 + Z_3 \cdot Z_1}{Z_2}$$

$$Z_c = \frac{Z_1 \cdot Z_2 + Z_2 \cdot Z_3 + Z_3 \cdot Z_1}{Z_3}$$