

NATIONAL EXAMS, DECEMBER 2018  
04-BS-9, BASIC ELECTROMAGNETICS  
3 HOURS DURATION

**NOTES:**

1. If doubt exists as to the interpretation of any question, the candidate is urged to submit with the answer paper, a clear statement of any assumptions made.
2. Candidates may use one of two calculators, the Casio or Sharp approved models. This is a closed book exam.
3. Any five questions constitute a complete paper. Only the first five questions as they appear in your answer book will be marked.
4. All questions are of equal value.
5. Aids:  $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$ ,  $\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$ ,  $e = 1.6 \times 10^{-19} \text{ C}$

1. In a parallel plate capacitor plate separation  $d$  is 1mm and circular plate area is  $5 \text{ cm}^2$ . A Cartesian  $z$  - coordinate perpendicular to the plates is established with  $z = 0$  located on one of the plates, the  $z$  - coordinate of the other plate being  $d$ . Relative permittivity  $\epsilon$  of the dielectric filling completely the space between the plates is  $\epsilon = \epsilon_1 / (1 + \alpha z/2)$  with  $\epsilon_1 = 3$  and  $\alpha = 0.2/d$ .

What is the value of capacitance of the capacitor?

2. Inductance  $L$  of an air core tightly wound solenoid of  $N$  turns, length  $L$  and circular cross-section are  $A$  is  $L = \mu_0 N^2 A / L$  for the case of  $A/L^2 \ll 1$ . A magnetic cylinder of circular cross-section  $A$ , length  $L$  and relative permeability  $\mu = 20$  is inserted into the solenoid described above with portion of length  $L/2$  inside the solenoid and length  $L/2$  portion outside.

Calculate inductance of magnetic core solenoid described above.

3. A layer of current flows below the horizontal flat surface of a metallic plate of infinite dimension. The current and associated current densities are uniform in horizontal directions but vary from maximum at the metallic surface to zero,  $10^{-5} \text{ m}$  below the surface. The total linear current is  $.05 \text{ A/m}$  and the direction of the flow is north.

What are the values and direction of the magnetic flux density  $B$  on the surface of the metal and  $10^{-5} \text{ m}$  below it?

4. Two positive point charges  $+Q$  are  $10^{-10} \text{ m}$  apart. A negative charge  $-q$  is located at midpoint of the two positive charge locations.

For what minimum value of absolute value of  $q$  will the mutual repulsion of the two positive charges be eliminated?

5. A straight horizontal metallic rod 2m long is aligned in the  $30^\circ$  north of east direction. It is moving in the horizontal, north direction at 50 m/s velocity in a vertical magnetic field of  $10^{-5}$  teslas pointing up.

What are the magnitude and polarity of the voltage induced between the tips of the rod?

6. A plane wave of  $10^{10}$ Hz frequency is incident at a  $45^\circ$  angle on the horizontal surface of water. Relative permittivity of water at that frequency is approximately 81.

Determine the directions of reflected and penetrating waves and their wavelengths.

7. A 2A current loop consists of three quarter circles, one lying in the positive x - y plane a Cartesian x-y-z coordinate system, one in the positive y-z plane and one in the positive z-x plane. Centers of the three quarter circles are in the origin of the coordinate system and their common radius is 10 cm.

What is the magnitude of the magnetic flux density B at the center of the loop?

8. A beam of electrons accelerated by  $10^4$ V is moving horizontally in the east direction. It is deflected by an electric field of  $10^6$  V/m pointing down. The electric deflecting force is cancelled by a magnetic field.

What is the magnitude and direction of the magnetic flux density value of the field?