

# National Exams December 2018

16-Mex-A2, Circuits and Electronics

3 hours duration

## NOTES:

1. If doubt exists as to the interpretation of any question, the candidate is urged to submit with the answer paper, a clear statement of any assumptions made.
2. This is a CLOSED BOOK EXAM. An approved Casio or Sharp model calculator is permitted.
3. This exam **has two parts Part A Circuits and Part B Electronics**. Answer either 3 questions from Part A and two questions from Part B or 2 questions from Part A and 3 questions from Part B a total of 5 questions answered. Indicate in the front page of your answer book which questions you want to be marked.
4. Please indicate which part the question you are answering is from either Part A or Part B. Start each new question on a new page and number and part number e.g. Q4(a).
5. For the Part B Electronics part of the exam in schematics, ground and chassis may be assumed to be common, unless specifically stated otherwise. Also, unless otherwise specified, assume that Op-Amps are ideal and that supply voltages are
6. If questions require an answer in essay format, clarity and organization of the answer are important. Provide block diagrams and circuit schematics whenever necessary.
7. For the Part A Circuits part of the exam some useful equations and transforms are provided.
8. All questions are of equal value. Part Marks will be given for right procedures.

16-MEX-A2

PART A

CIRCUITS

ANSWER A MAXIMUM OF 3 QUESTIONS FROM THIS  
PART A SECTION AND TWO QUESTIONS FROM THE  
PART B SECTION

OR

ANSWER 2 QUESTIONS FROM THIS PART A SECTION  
AND 3 QUESTIONS FROM THE PART B SECTION

Q1: For the circuit shown in Figure-1,

(a) Calculate the equivalent resistance of the circuit,  $R_{AB}$  at the terminals A and B. [10]

(b) Solve for the current  $I$  at the location shown. [5]

(c) Calculate the Power dissipation in the  $12\Omega$  resistance. [5]

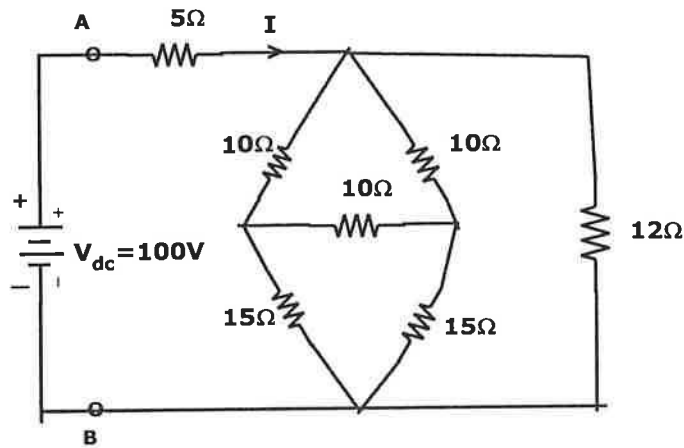


Figure-1

Q2: In the Figure-2 solve the voltage,  $V_o$  by the Superposition theorem. [20]

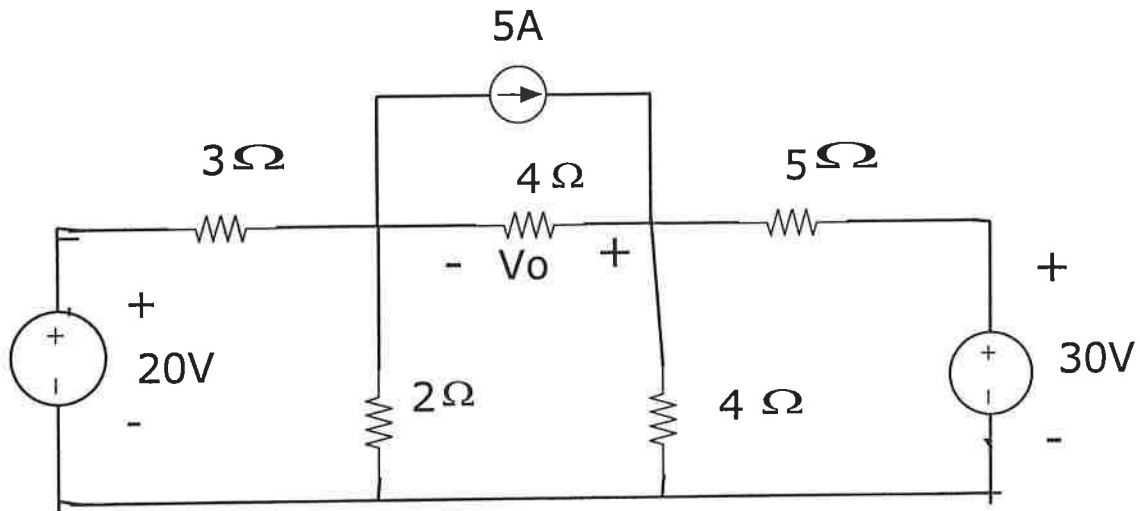


Figure-2

Q3: In Figure-3, the switch was in position-A for a long time. At  $t = 0$ , it is moved to Position-B.

Calculate (i)  $v_c(0+)$ ,  $\frac{dv_c}{dt}(0+)$ , and  $v_c(\infty)$  [4+6+2]

(ii)  $v_c(t)$  when  $t \geq 0$  [8]

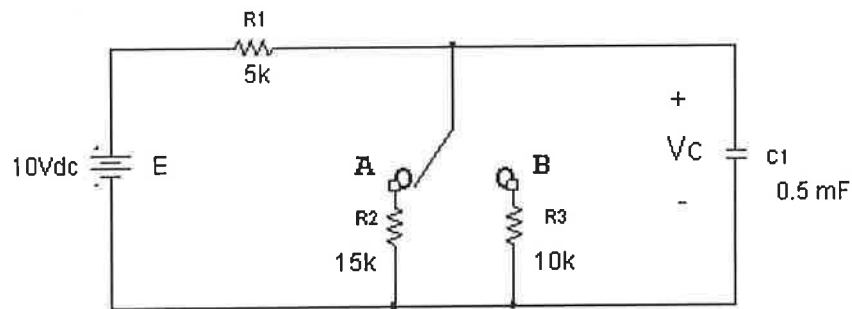


Figure-3

Q4: (a) For the circuit shown in Figure-4, calculate the load resistance  $R_L$  to be connected across the terminals a and b for maximum power dissipation. [10]

(b) Calculate this maximum possible power dissipation in  $R_L$ . [10]

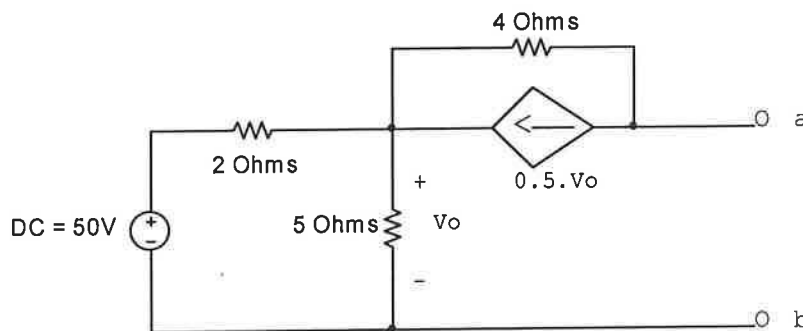


Figure-4

- Q5: (a) Write the Node Voltage equations of the following ac circuit, Figure-5, where the frequency is 60 Hz. [8]
- (b) Solve the node voltages, and calculate the power supplied by the voltage source, e. [6+6]

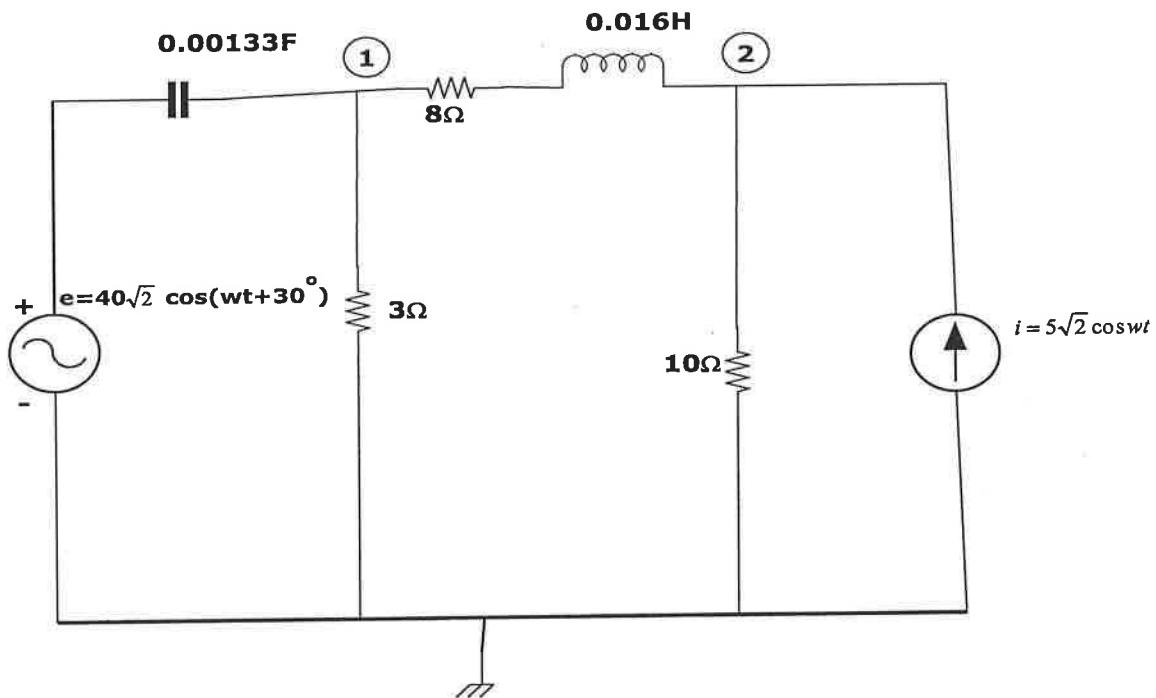


Figure-5

- Q6: (a) In the circuit shown in Figure-6, the switch was on position-a for a long time. At  $t = 0$ , the switch is moved to position-b. Calculate  $V_c(0^+)$  and  $i(0^+)$ . [4]
- (b) Draw the Laplace Transformed circuit at  $t \geq 0$ . [8]
- (c) Solve  $V_c(t)$ . [8]

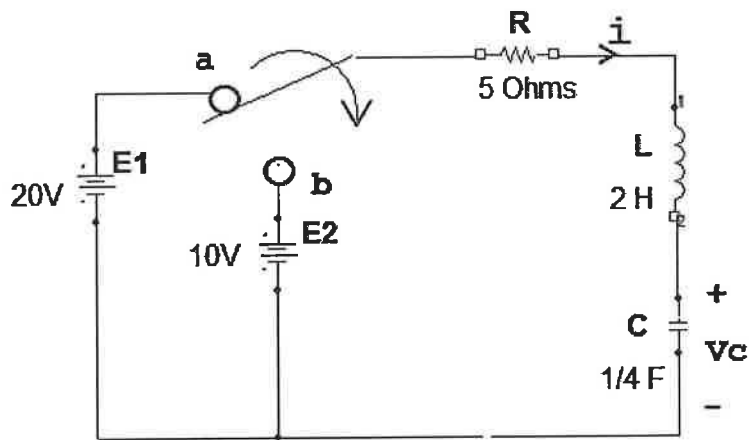
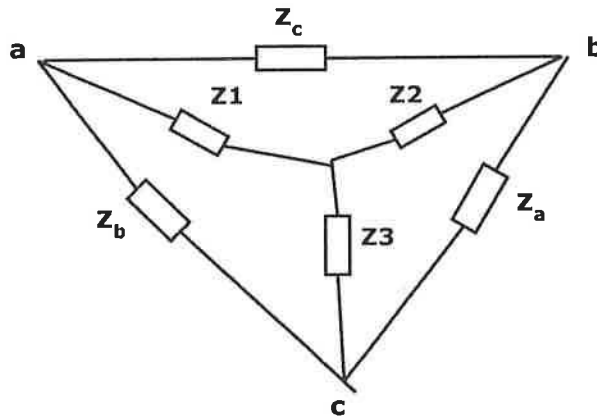


Figure-6

### Appendix

Some useful Laplace Transforms:

<u>f(t)</u>	→	<u>F(s)</u>
$Ku(t)$		$K / s$
$\delta(t)$		$1$
$t$		$1/s^2$
$e^{-at} u(t)$		$1 / (s+a)$
$\sin \omega t \cdot u(t)$		$\omega / (s^2+\omega^2)$
$\cos \omega t \cdot u(t)$		$s / (s^2+\omega^2)$
$e^{-at} \sin \omega t$		$\frac{\omega}{(s+\alpha)^2+\omega^2}$
$e^{-at} \cos \omega t$		$\frac{(s+\alpha)}{(s+\alpha)^2+\omega^2}$
$\frac{df(t)}{dt}$		$s F(s) - f(0^-)$
$\frac{d^2 f(t)}{dt^2}$		$s^2 F(s) - s f(0^-) - f'(0^-)$
$\int_{-\infty}^t f(q) dq$		$\frac{F(s)}{s} + \int_{-\infty}^0 f(q) dq$

Star – Delta conversion:

$$Z_1 = \frac{Z_b \cdot Z_c}{Z_a + Z_b + Z_c}$$

$$Z_2 = \frac{Z_a \cdot Z_c}{Z_a + Z_b + Z_c}$$

$$Z_3 = \frac{Z_a \cdot Z_b}{Z_a + Z_b + Z_c}$$

$$Z_a = \frac{Z_1 \cdot Z_2 + Z_2 \cdot Z_3 + Z_3 \cdot Z_1}{Z_1}$$

$$Z_b = \frac{Z_1 \cdot Z_2 + Z_2 \cdot Z_3 + Z_3 \cdot Z_1}{Z_2}$$

$$Z_c = \frac{Z_1 \cdot Z_2 + Z_2 \cdot Z_3 + Z_3 \cdot Z_1}{Z_3}$$



16-MEX-A2

PART B  
ELECTRONICS

ANSWER A MAXIMUM OF 3 QUESTIONS FROM THIS  
PART B SECTION AND TWO QUESTIONS FROM THE  
PART A SECTION

OR

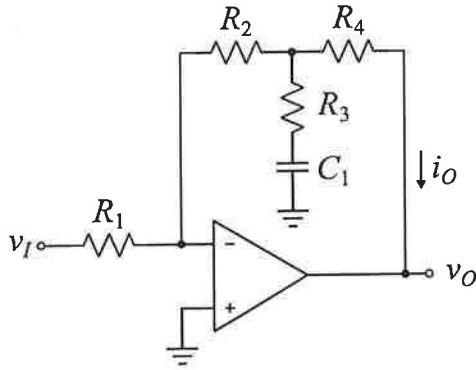
ANSWER 2 QUESTIONS FROM THIS PART B SECTION  
AND 3 QUESTIONS FROM THE PART A SECTION

**QUESTION (7)**

The op amp in the following circuit is ideal except for an input offset voltage of  $\pm 3 \text{ mV}$ .

a) What is the output DC offset voltage? (8 point)

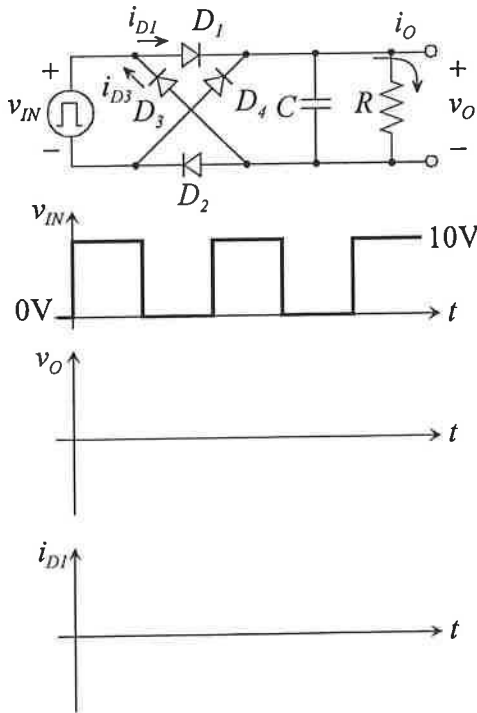
b) What is the small signal voltage gain  $v_o/v_i$ ? (12 point)



Given:  $R_1 = R_2 = R_4 = 100 \text{ k}\Omega$   
 $R_3 = 1 \text{ k}\Omega$   
 $C_1 = \text{very large}$

**QUESTION (8)**

The diodes are ideal except with an on-voltage of  $0.7 \text{ V}$ . The input voltage source  $v_{IN}$  is a  $100 \text{ Hz}$ ,  $50\%$  duty cycle square-wave with voltage levels of  $0 \text{ V}$  and  $+10 \text{ V}$ . The load resistance,  $R = 100 \Omega$ .



a) If the ripple voltage,  $V_r = 0.5 \text{ V}$ , sketch the output waveform for several input cycles. What is the average DC output voltage  $v_o$ . (6 points)

b) What would be the minimum value of  $C$  (in  $\mu\text{F}$ ) required to keep  $V_r \leq 0.5 \text{ V}$ ? (4 points)

c) Sketch the current waveform for  $i_{D1}$  flowing through diode  $D_1$ . Indicate the time interval that the capacitor is charging. (6 points)

d) What is the overall average current ( $i_{D3}$ ) flowing through diode  $D_3$ ? (4 points)

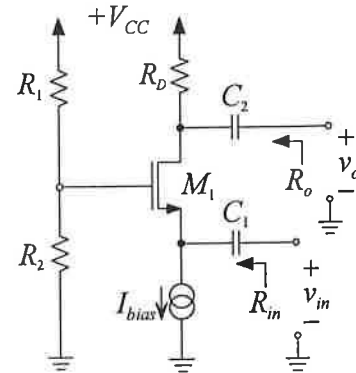
**QUESTION (9)**

Transistor  $M_1$  in this common gate amplifier circuit has the following characteristics:

$$V_{TH} = 1 \text{ V}$$

$$K = 1 \text{ mA/V}^2 \quad \lambda = 0.1$$

Given:  $V_{DD} = 10 \text{ V}$ ,  $I_{bias} = 2 \text{ mA}$ ,  
 $C_1 = C_2 = \infty$ ,  
 $R_1 = 10 \text{ k}\Omega$ ,  $R_2 = 5 \text{ k}\Omega$ ,  $R_D = 2 \text{ k}\Omega$



- a) Determine the small signal gain,  $v_o/v_{in}$ . (12 points)
- b) Determine the input resistance,  $R_{in}$ . (4 points)
- c) Determine the output resistance,  $R_o$ . (4 points)

Useful formulae: for n-channel MOSFET

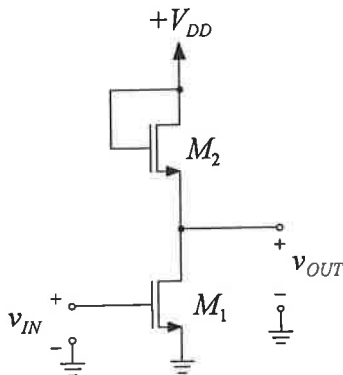
$$i_{DS} = K \left[ (v_{GS} - V_{TH})v_{DS} - \frac{1}{2}v_{DS}^2 \right] \quad \text{triode region}$$

$$i_{DS} = \frac{1}{2}K (v_{GS} - V_{TH})^2 (1 + \lambda v_{DS}) \quad \text{saturation region}$$

**QUESTION (10)**

This is an enhancement load NMOS inverter. Given that the transistors are identical,

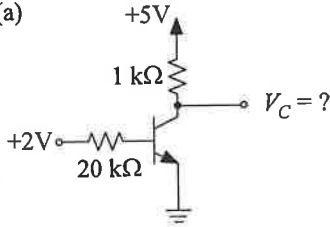
- a) Draw the input to output voltage transfer characteristic (VTC) for this inverter. Express and label clearly all voltage levels on the VTC plot. (12 points)
- b) Indicate the noise margins  $NM_L$  and  $NM_H$  on the VTC. (2 points)
- c) Indicate the logic high and low output voltage levels  $V_{OH}$ ,  $V_{OL}$  on the VTC. (2 points)
- d) Indicate the logic high and low input voltage levels  $V_{IH}$ ,  $V_{IL}$  on the VTC. (2 points)
- e) Indicate clearly the mode of operation for transistors  $M_1$  and  $M_2$  in each region of the VTC. (2 points)



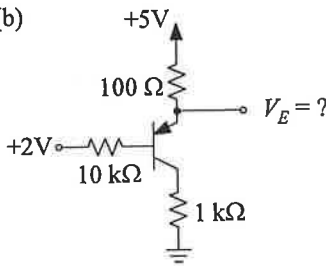
**QUESTION (11)**

In this question, all BJT transistors have  $\beta = 50$ ,  $V_{BE,on}$  or  $V_{EB,on} = 0.6V$ ,  $V_{CE,sat}$  or  $V_{EC,sat} = 0.3V$  and  $V_A = \infty$ . Solve for the required voltages. (20 points)

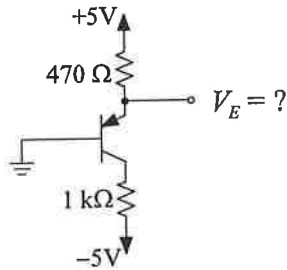
(a) (4 points)



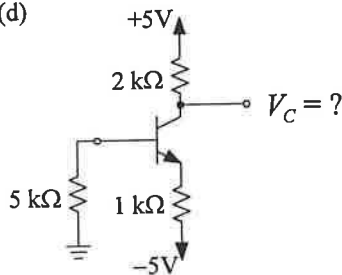
(b) (4 points)



(c) (4 points)



(d) (4 points)



(e) (4 points)

