# NATIONAL EXAMS MAY 2017

98-Phys-A5: Semiconductor Devices &

Circuits Duration: 3 hours

### **NOTES:**

- 1. If doubt exits as to the interpretation of any question, the candidate must submit with the answer paper, a clear statement of any assumption(s) made.
- 2. Candidates may use one of two calculators, the Casio or Sharp approved models.
- 3. This is a **CLOSED BOOK EXAM.**Useful constants and equations have been annexed to the exam paper.
- 4. Any FIVE (5) of the SEVEN (7) questions constitute a complete exam paper. The first five questions as they appear in the answer book will be marked.
- 5. When answering questions, candidates **MUST** clearly indicate units for all parameters used or computed.

#### MARKING SCHEME

Questions	Marks				
1	(a) 3	(b) 3	(c) 5	(d) 5	(e) 4
2	(a) 3	(b) 6	(c) 4	(d) 7	
3	(a) 4	(b) 4	(c) 6	(d) 6	
4	(a) 3	(b) 3	(c) 5	(d) 4	(e) 5
5	(a) 8	(b) 5	(c) 2	(d) 5	
6	(a) 3	(b) 6	(c) 6	(d) 5	
7	(a) 8	(b) 8	(c) 4		

- 1. Figure P1 shows a silicon bar of length L and cross-sectional area of  $100 \ \mu m^2$  connected in series with a 10V battery. The bar is doped with  $10^{17}$  donor atoms/cm<sup>3</sup>. At  $300 \ ^{\circ}$ K, this corresponds to an electron mobility of  $700 \ cm^2/V$ -s and electron drift velocity saturation of  $10^7 \ cm/s$  for any electrical field E exceeding  $E_{sat} = 10^4 \ V/cm$ .
- <sup>3</sup> pts (a) Briefly explain why electron mobility would decrease if the donor concentration was augmented.
- (b) Briefly explain why electron drift velocity saturates in the presence of high electrical fields.
- <sup>5 pts</sup> (c) Estimate the current I in the bar when its length L = 0.1 cm.
- <sup>5 pts</sup> (d) Estimate the current I in the bar when its length  $L = 0.5 \mu m$ .
- 4 pts (e) Evaluate the Hall coefficient of the semiconductor bar.

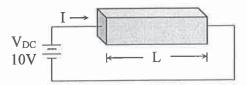
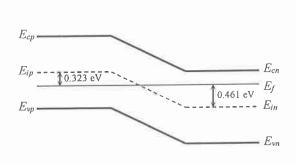


Figure P1

2. A diode is fabricated by using an abrupt silicon P-N<sup>+</sup> junction formed by merging P-type and N-type semiconductors of constant cross section  $A = 10^{-4}$  cm<sup>2</sup>. The device is used in an ambient temperature of T = 300 °K. The equilibrium band diagram and current-voltage characteristic of the diode are shown at the right-hand side of Figure P2. The basic properties of the P-type and N-type semiconductors for a temperature of T = 300 °K are shown in the table below.

P type	N type		
$p_i = 2 \times 10^{10} \text{ cm}^{-3}$	$n_i = 2 \times 10^{10} \text{ cm}^{-3}$		
$\tau_n = 0.1 \mu s$	$\tau_p = 10 \ \mu s$		
$\mu_p = 200 \text{ cm}^2/(\text{V-s})$	$\mu_n = 1300 \text{ cm}^2/(\text{V-s})$		
$\mu_n = 700 \text{ cm}^2/(\text{V-s})$	$\mu_p = 450 \text{ cm}^2/(\text{V-s})$		

- (a) Based on the band diagram, what is the value of the contact potential of the P-N junction?
- (b) Evaluate the concentration of majority carriers, pp and nn, on each side of the P-N junction.
- 4 pts (c) Evaluate the concentration of minority carriers, np and pn, on each side of the P-N junction.
- 7 pts (d) If the impurity concentrations are adjusted such that  $n_p = 1.35 \times 10^5$  cm<sup>-3</sup> and  $p_n = 324$  cm<sup>-3</sup> what is the value of the reverse saturation current of the P-N junction?



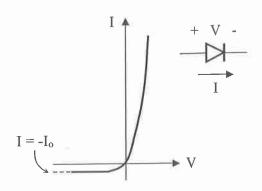


Figure P2

- 3. A second order high-pass active filter circuit is shown in Figure P3.
- 4 pts (a) List two advantages of active filters?
- (b) If the OP amps are considered ideal, what are the values of input impedance R<sub>in</sub> and output impedance R<sub>out</sub>?
- 6 pts (c) Show that the filter transfer function is given by

$$F(s) = \frac{V_3(s)}{V_1(s)} = \frac{10 s^2}{s^2 + 2\omega_o s + \omega_o^2}$$

where the natural frequency of the filter is given by  $\omega_o = 1/RC$ .

(d) Evaluate the magnitude of F(s) in dB and the phase shift of F(s) in degrees of this filter when the frequency of the input signal is  $\omega = 0.5 \omega_0$ .

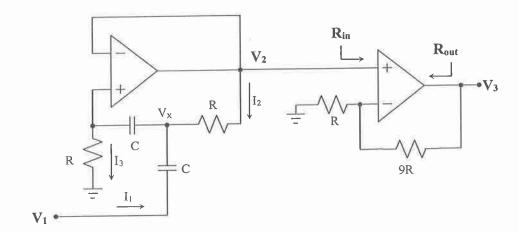


Figure P3

4. A single stage small signal amplifier is shown in Figure P4. The MOSFET device in the circuit needs to be biased such that the DC drain current  $I_D = 1$  mA and drain-source voltage  $V_{DS} = 10$  V. To obtain these values, the gate-source voltage must be set to  $V_{GS} = 1$  V. At that operating point, the small signal parameters of the device are  $g_m = 4$  mA/V and  $r_o = 500$  k $\Omega$ . The low frequency response of this amplifier is given by

$$G_L(s) = A_{vm} \frac{s}{(s + \omega_{p1})} \frac{(s + \omega_z)}{(s + \omega_{p2})} \frac{s}{(s + \omega_{p3})}$$

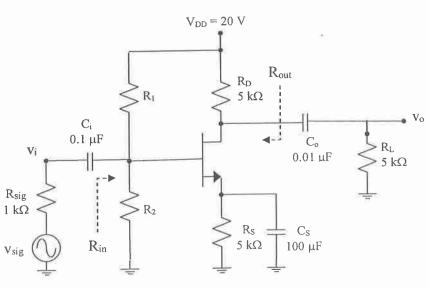
where  $A_{vm}$  is the midband voltage gain, and

$$\omega_{z} = \frac{1}{R_{s}C_{s}} \qquad \omega_{p1} = \frac{1}{(R_{sig} + R_{in})C_{i}} \qquad \omega_{p2} = \frac{1}{(R_{s} \| \frac{1}{g_{m}})C_{s}} \qquad \omega_{p3} = \frac{1}{(R_{out} + R_{L})C_{o}}$$

- 3 pts (a) Briefly explain the main purpose of using capacitor C<sub>s</sub> in the circuit of Figure P4.
- 3 pts (b) Draw the midband small signal equivalent circuit of the amplifier and show that the output resistance  $\mathbf{R}_{out}$  of the amplifier is equal to 4.95 k $\Omega$ .
- 5 pts (c) Select suitable values for resistors R<sub>1</sub> and R<sub>2</sub> to meet the following requirements:

$$V_{GS} = 1~V$$
 and  $R_{in} = 420~k\Omega$ 

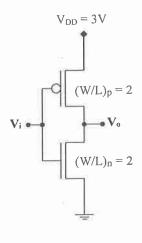
- 4 pts (d) Calculate the midband voltage gain  $A_{vm} = v_0/v_{sig}$ .
- (e) If the high frequency response of this amplifier is given by  $G_H(s) = A_{vm} \frac{1}{(1+s/\omega_H)} \text{ where } \omega_H = 90 \text{ krad/s},$  evaluate the bandwidth of this amplifier.



- 5. Figure P5a shows a CMOS inverter circuit and its related voltage transfer characteristic (VTC). Figure P5b shows a ring oscillator built with five identical versions of the same CMOS inverter.
- (a) From the VTC shown in Figure P5a, graphically extract approximate values for: 8 pts
  - i. the LOW noise margin NML;
  - ii. the HIGH noise margin NMH;
  - iii. the switching voltage V<sub>x</sub>; and
  - iv. the small signal gain.

Briefly explain how each of the four parameters was graphically extracted.

- (b) Calculate the exact value of the switching voltage if fabrication parametric measurements show 5 pts that  $k_n = 3k_p$ ,  $V_{tn} = 0.4$  V and  $V_{tp} = -0.5$  V.
- (c) Briefly explain how the inverter circuit could be modified to make the switching voltage equal 2 pts to 1.5V (half the supply voltage V<sub>DD</sub>).
- (d) If the inverter is designed with timing parameters  $t_{phl}$  and  $t_{plh}$  that are equal to 1.8 ns and 2.2 ns 5 pts respectively, calculate the frequency of output signal v(t) coming out of node N of the ring oscillator circuit shown in Figure P5b.



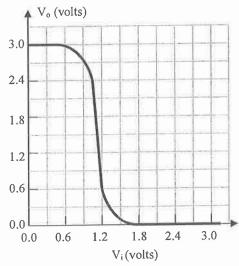


Figure P5a

- 6. The circuit displayed in Figure P6 receives a rapidly changing audio signal S(t) and uses a three-stage *n*-bit analog-to-digital converter (ADC) to provide a digital signal to a processor. Maximum delays of major components of the ADC are also shown. The input signal amplitude range is 0 ≤ S(t) ≤ 3 V.
- 3 pts (a) State the name of the type of ADC circuit used <u>and</u> state its main disadvantage and its main advantage.
- (b) If  $V_{ref} = 3.1 \text{ V}$ , determine the minimum number of bits *n* required to code the digital signal to obtain a resolution of at least 0.025 V.
- (c) If the ADC is designed with n = 8, what would be the value of the binary (hexadecimal) code sent to the processor when the amplitude of S(t) = 2 V?
- 5 pts (d) What is the maximum speed (frequency) of conversion of this ADC?

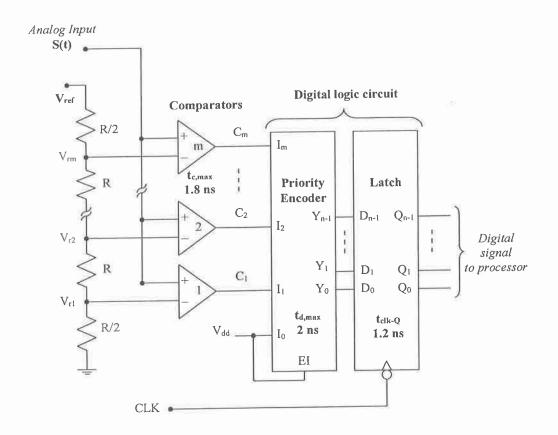


Figure P6

- 7. Figure P7 shows the basic diagram of a precision bridge rectifier for instrumentation applications. The OP amp is assumed to be ideal. The meter M has a coil resistance of  $r = 100 \Omega$  and provides a full-scale deflection when the *average current* through it is 2 mA.
- 8 pts (a) Find the value of R to provide a full-scale reading when the input voltage is a sine wave of amplitude equal to 5 V.
- 8 pts (b) At full-scale reading, and assuming the diodes have a 0.5 V forward voltage drop, evaluate how far the maximum value of V<sub>C</sub> is from the saturation level of the OP amp.
- 4 pts (c) If an engineer decides to use diodes with a peak reverse voltage (PRV) rating equal to 1 V, determine if this rating is sufficient to prevent junction breakdown at full-scale reading.

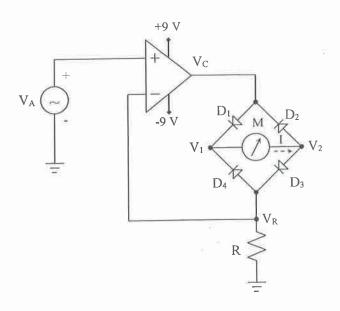


Figure P7

# ANNEX: USEFUL CONSTANTS, EQUATIONS and MODELS

(1) 
$$1 \stackrel{\circ}{A} = 10^{-10} \text{ m} = 10^{-8} \text{ cm} = 10^{-4} \text{ } \mu\text{m}$$

- (2)  $q = 1.6 \times 10^{-19} \text{ C}$
- (3)  $k = 1.38 \times 10^{-23} \text{ J/°K} = 8.62 \times 10^{-5} \text{ eV/°K}$  [At T = 300°K, kT = 0.026 eV,  $V_T = kT/q \approx 26 \text{ mV}$ ]
- (4) Decibel:  $20 \log_{10} (V_2/V_1)$  for a voltage ratio;  $10 \log_{10} (P_2/P_1)$  for a power ratio

(5) For silicon (Si) at 
$$T = 300 \text{ °K}$$
:  $n_i = 1.5 \times 10^{10} / \text{cm}^3$ 

- (6)  $\varepsilon_{\text{Si}} = 1.04 \times 10^{-12} \text{ F/cm}$
- (7)  $\varepsilon_{SiO2} = 0.345 \times 10^{-12} \text{ F/cm}$  [farad: 1 F = 1 C/V] [siemens: 1 mS = 1 mA/V = 1 mmho]

(8) 
$$f(E) = \frac{1}{1 + e^{(E - E_F)/kT}}$$

$$(9) \qquad n_o + N_a = p_o + N_d$$

(10) 
$$n_o p_o = n_i^2$$

(11) 
$$n_o = N_c e^{(E_F - E_c)/kT} = n_i e^{(E_F - E_i)/kT}$$

(12) 
$$p_o = N_v e^{(E_v - E_F)/kT} = n_i e^{(E_i - E_F)/kT}$$

(13) 
$$n_i = \sqrt{N_{\rm c} N_{\rm v}} \, {\rm e}^{-{\rm E}_{\rm g}/2kT}$$

(14) 
$$V_o = \frac{kT}{q} \ln \frac{N_a N_d}{n_i^2}$$

(15) 
$$W = \sqrt{\frac{2\varepsilon_{Sl}V_o}{q} \left(\frac{1}{N_a} + \frac{1}{N_d}\right)}$$

(16) 
$$x_{po} = \frac{W N_d}{N_a + N_d}$$
  $x_{no} = \frac{W N_a}{N_a + N_d}$ 

(17) 
$$E(x) = \int \frac{\rho(x)}{\varepsilon} dx \qquad \phi(x) = -\int E(x) dx$$

(18) 
$$\mu = \frac{v_{drift}}{\varepsilon}$$

(19) 
$$\sigma = q(n_o \mu_n + p_o \mu_p)$$

(20) 
$$\frac{D_{\rho}}{\mu_{p}} = \frac{D_{n}}{\mu_{n}} = \frac{kT}{q} \qquad L_{n} = \sqrt{D_{n}\tau_{n}} \qquad L_{\rho} = \sqrt{D_{p}\tau_{p}}$$

(21) 
$$n_n p_n = n_i^2 = n_p p_p$$

(22) 
$$I = I_o(e^{\frac{qV}{kT}} - 1) = qA \left(\frac{D_p}{L_p} p_n + \frac{D_n}{L_n} n_p\right) (e^{\frac{qV}{kT}} - 1)$$

$$(23) J = \frac{I}{A} = \sigma \mathcal{E}$$

(24) 
$$R = \frac{L}{\sigma A}$$

$$(25) R_H = \frac{1}{q(p_o - n_o)}$$

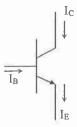
## BJT relationships and model

(26) 
$$I_C = \beta I_B$$
 where  $\beta = I_C/I_B$ 

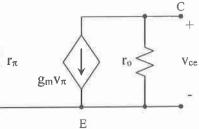
(27) 
$$I_E = I_B + I_C$$

$$(28) g_m = I_C/V_T$$

(29) 
$$r_{\pi} = V_{T}/I_{B}$$



mall signal  $V_{\pi}$ 



### MOS device in a p substrate

(30) 
$$\phi_F = \frac{kT}{q} \ln \frac{N_a}{n_i}$$

$$(31) W_m = 2\sqrt{\frac{\varepsilon_{Si}\phi_F}{qN_a}}$$

$$(32) Q_d = -qN_aW_m$$

$$(33) C_i = \frac{\varepsilon_{SiO_2}}{d}$$

(34) 
$$V_T = \Phi_{ms} + 2\phi_F - \frac{1}{C_i}(Q_i + Q_d)$$

# MOSFET symbols, relationships and model

$$(35) g_m = \frac{\partial I_D}{\partial V_{GS}}$$

(36) 
$$k_n = \mu_n C_{ox}(W/L)_n$$

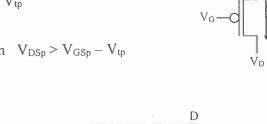
(37) 
$$k_p = \mu_p C_{ox}(W/L)_p$$

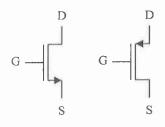
$$(38) \qquad I_{\text{Dn}} = (k_{\text{n}}/2) \; (V_{\text{GSn}} - V_{\text{tn}})^2 \qquad \text{when} \; \; V_{\text{DSn}} > V_{\text{GSn}} - V_{\text{in}}$$

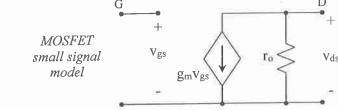
(39)  $I_{Dn} = (k_n/2) \left[ 2(V_{GSn} - V_{tn})(V_{DSn}) - (V_{DSn})^2 \right] \quad \text{when} \quad V_{DSn} < V_{GSn} - V_{tn}$ 

(40) 
$$I_{Dp} = (k_p/2) (V_{GSp} - V_{tp})^2$$
 when  $V_{DSp} < V_{GSp} - V_{tp}$ 

(41) 
$$I_{Dp} = (k_p/2) \left[ 2(V_{GSp} - V_{tp})(V_{DSp}) - (V_{DSp})^2 \right]$$
 when  $V_{DSp} > V_{GSp} - V_{tp}$ 







- (42) For a complex number R = A + Bj,  $|R| = (A^2 + B^2)^{1/2}$  and  $\phi(R) = tan^{-1}(B/A)$
- (43)  $V_o(t) = -\frac{1}{RC} \int_0^T V_i(t) dt$   $\frac{V_o(s)}{V_i(s)} = \frac{-1}{sRC}$  [integrator circuit]
- (44)  $V_{DC} \equiv V_{average} = \frac{1}{T} \int_{0}^{T} V(t) dt = V_{p}/\pi$  for a half-wave sinewave and  $2V_{p}/\pi$  for full-wave sinewave
- (45)  $V_{rms} = \sqrt{\frac{1}{T} \int_{0}^{T} [V(t)]^2 dt}$   $= \frac{V_p}{2}$  for a half-wave sinewave and  $\frac{V_p}{\sqrt{2}}$  for full-wave sinewave